## Scale and Weight Problem

What is the minimum number of weights that can be used on a scale pan to weight any integral number of pounds from one to ten inclusively, if the weights can be placed in either pan?

## Things to Consider



- For each weight, there are three things you can do with it:
- put it on the left pan
- put it on the right pan
- not put it on the balance at all
$\square \quad$ Weights can be used to make other weights and they can cancel each other out, for example, 2 and 5 can be used to make 7 (have both on the same scale pan) or 3 (have 2 on one scale pan and 5 on the other)

Answers

| Number | Scale Pan 1 | Scale Pan 2 |
| :---: | :---: | :---: |
| 1 | 1 | 0 |
| 2 | 1 | 3 |
| 3 | 3 | 0 |
| 4 | $1+3$ | 0 |
| 5 | $1+3$ | 9 |
| 6 | 3 | 9 |
| 7 | $1+9$ | 3 |
| 8 | 9 | 1 |
| 9 | $1+9$ | 0 |
| 10 |  | 0 |

## Answer

| Number | Scale Pan 1 | Scale Pan 2 |
| :---: | :---: | :---: |
| 1 | 1 | 0 |
| 2 | 1 | 3 |
| 3 | 3 | 0 |
| 4 | $1+6$ | 3 |
| 5 | 1 | 6 |
| 6 | 6 | 0 |
| 7 | $1+6$ | 0 |
| 8 | $1+6$ | $3+6$ |
| 9 | $1+6$ | 0 |
| 10 |  |  |

